

| item | bid value | status     |
|------|-----------|------------|
| 1    | 93        | SELECTED   |
| 2    | 43        | UNSELECTED |
| 3    | 21        | SELECTED   |
| 4    | 17        | UNSELECTED |
| 5    | 29        | UNSELECTED |

edit constraint

| •  |            | 1 - 1 | 1 4         |
|----|------------|-------|-------------|
| ha | CIC        | hid   | <b>dota</b> |
| va | <b>316</b> | DIU   | data        |

| Set |        | budget |     |
|-----|--------|--------|-----|
|     | 1, 2,3 |        | 120 |
|     | 3,4,5  |        | 50  |

budget constraints

|   | precedence |
|---|------------|
|   | set        |
| 3 | 1          |
| 3 | 2,4        |
|   | 3          |

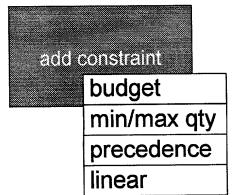
| min qty | set     | max qty |
|---------|---------|---------|
| 2       | 1,2,3,4 |         |
|         | 2,4,5   | 2       |

quantity constraints

recedence constraints

| item  | coef | coef |
|-------|------|------|
| 1     | 10   | 10   |
| 2     | 10   | -10  |
| 3     | 20   | 10   |
| 4     | 40   | -10  |
| 5     |      | 10   |
| total | 60   | 20   |

linear constraints



| item |   | bid value | status     |
|------|---|-----------|------------|
|      | 3 | 43        | UNSELECTED |
|      | 4 | 29        | SELECTED   |
|      | 5 | 31        | SELECTED   |
|      | 6 | 12        | SELECTED   |
|      | 7 | 17        | UNSELECTED |

basic bid data

| W. I. W. | WWW.   | train |  |
|----------|--------|-------|--|
|          | oviec. |       |  |
|          |        |       |  |
|          |        |       |  |
|          |        |       |  |
|          |        |       |  |
|          |        |       |  |
| <br>     |        |       |  |

| Set   | budget |
|-------|--------|
| 5,6,7 | 50     |

budget constraints

add bid

| item  | coef | coe | f  |
|-------|------|-----|----|
|       | 3    | 20  | 15 |
| 100   | 4    | 30  | 18 |
|       | 5    | 21  | 13 |
|       | 6    |     | 17 |
|       | 7    | 30  | 14 |
| total |      | 50  | 48 |

linear constraints

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#### Fig. 3a (numeral 34)

Max 
$$93x_{1,1} + 43x_{1,2} + 21x_{1,3} + 17x_{1,4} + 29x_{1,5} + 43x_{2,3} + 29x_{2,4} + 31x_{2,5} + 12x_{2,6} + 17x_{2,7}$$
  
Subject to  $x_{3,1} + x_{3,2} \le 1$   
 $x_{4,1} + x_{4,2} \le 1$ 

$$93x_{1,1} + 43x_{1,2} + 21x_{1,3} \le 120$$

$$21x_{1,3} + 17x_{1,4} + 29x_{1,5} \le 50$$

$$x_{1,2} + x_{1,4} + x_{1,5} \le 2$$

 $x_{5,1} + x_{5,2} \le 1$ 

$$2z_{1,1}^{Min} \le x_{1,1} + x_{1,2} + x_{1,3} + x_{1,4}$$

$$x_{1,1} \le z_{1,1}^{Min}$$

$$x_{1,2} \leq z_{1,1}^{Min}$$

$$x_{1,3} \le z_{1,1}^{Min}$$

$$x_{1,3} \le z_{1,3,1}^P + z_{1,3,2}^P$$

$$z_{1,3,1}^P \leq x_{1,1}$$

$$2z_{1,3,2}^P \le x_{1,2} + x_{1,4}$$

$$10x_{1,1} + 10x_{1,2} + 20x_{1,3} + 40x_{1,4} \le 60$$

$$10x_{1,1} - 10x_{1,2} + 10x_{1,3} - 10x_{1,4} + 10x_{1,5} \le 20$$

$$31x_{2,5} + 12x_{2,6} + 17x_{2,7} \le 50$$

$$20x_{2,3} + 30x_{2,4} + 21x_{2,5} + 30x_{2,7} \le 50$$

$$15x_{2,3} + 18x_{2,4} + 13x_{2,5} + 17x_{2,6} + 14x_{2,5} \le 48$$

$$x_{1,1}, x_{1,2}, x_{1,3}, x_{1,4}, x_{1,5} \in \{0, 1\}$$

$$x_{2,3}, x_{2,4}, x_{2,5}, x_{2,6}, x_{2,7} \in \{0, 1\}$$

$$z_{1,1}^{Min}, z_{1,3,1}^P, z_{1,3,2}^P \in \{0,1\}$$

#### Fig. 3b (numeral 36)

$$\begin{aligned} &\textit{Max}\ 29y_{1,1} + 114y_{1,2} + 60y_{1,4} + 72y_{1,5} + 46y_{1,6} + 153y_{1,7} + 165y_{1,8} + 139y_{1,9} + \\ &43y_{2,1} + 29y_{2,2} + 31y_{2,3} + 12y_{2,4} + 17y_{2,5} + 55y_{2,8} + 60y_{2,9} + 60y_{2,10} + 41y_{2,11} + 104y_{2,14} + 72y_{2,15} \end{aligned}$$
 Subject to 
$$y_{1,1} + y_{1,2} + y_{1,4} + y_{1,5} + y_{1,6} + y_{1,7} + y_{1,8} + y_{1,9} \le 1$$
 
$$y_{2,1} + y_{2,2} + y_{2,3} + y_{2,4} + y_{2,5} + y_{2,8} + y_{2,9} + y_{2,10} + y_{2,11} + y_{2,14} + y_{2,15} \le 1$$
 
$$y_{1,2} + y_{2,1} + y_{2,8} + y_{2,9} + y_{2,14} + y_{2,15} \le 1h$$
 
$$y_{2,4} + y_{1,6} + y_{1,7} + y_{1,9} + y_{2,2} + y_{2,10} + y_{2,11} + y_{2,14} \le 1$$
 
$$y_{1,1} + y_{1,5} + y_{1,6} + y_{1,8} + y_{1,9} + y_{2,3} + y_{2,10} + y_{2,14} \le 1$$
 
$$y_{1,1}, y_{1,2}, y_{1,4}, y_{1,5}, y_{1,6}, y_{1,7}, y_{1,8}, y_{1,9}, y_{2,1} \in \{0, 1\}$$
 
$$y_{2,2}, y_{2,3}, y_{2,4}, y_{2,5}, y_{2,8}, y_{2,9}, y_{2,10}, y_{2,11}, y_{2,14}, y_{2,15} \in \{0, 1\}$$

The first constraint selects at most one proposal from player 1;

The second constraint selects at most one proposal from player 2;

The third constraint selects at most one proposal that includes item 3;

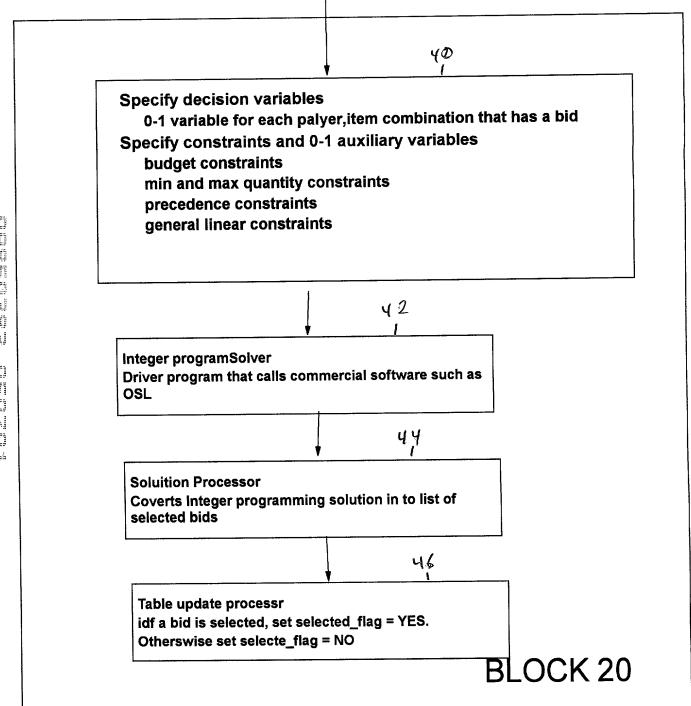
The fourth constraint selects at most one proposal that includes item 4;

The fifth constraint selects at most one proposal that includes item 5;

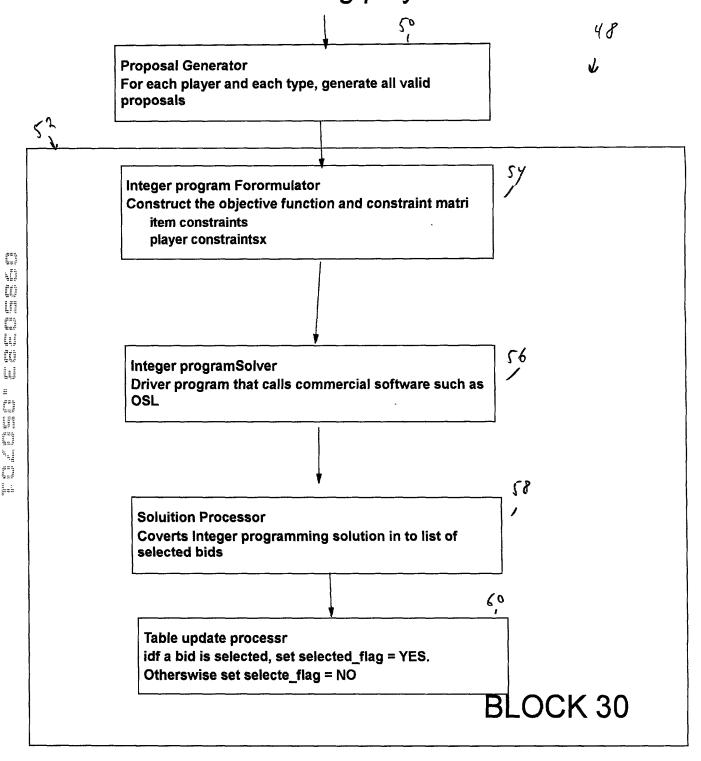
Constraints for items 1,2,6, and 7 are not required in this example, because only one player bids on each of these items and so the item constraint is implied by the player constraint.

## Bid data Including player constraints

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### Bid data Including player constraints



| proposal | Items   | Value | Reject ? |
|----------|---------|-------|----------|
| 1        | 5       | 29    |          |
| 2        | 1,3     | 114   |          |
| 3        | 1,5     | 122   | YES      |
| 4        | 2,4     | 60    |          |
| 5        | 2,5     | 72    |          |
| 6        | 4,5     | 46    |          |
| 7        | 1,2,4   | 153   |          |
| 8        | 1,2,5   | 165   |          |
| 9        | 1,4,5   | 139   |          |
| 10       | 1,2,3,5 | 182   | YES      |

# player 1's proposals

| proposal | Items | Value | Reject? |
|----------|-------|-------|---------|
| 1        | 3     | 43    |         |
| 2        | 4     | 29    |         |
| 3        | 5     | 31    |         |
| 4        | 6     | 12    |         |
| 5        | 7     | 17    |         |
| 6        | 3,4   | 72    | YES     |
| 7        | 3,5   | 74    | YES     |
| 8        | 3,6   | 55    |         |
| 9        | 3,7   | 60    |         |
| 10       | 4,5   | 60    |         |
| 11       | 4,6   | 41    |         |
| 12       | 5,6   | 43    | YES     |
| 13       | 6,7   | 29    | YES     |
| 14       | 3,4,5 | 104   |         |
| 15       | 3,6,7 | 72    |         |

player 2's proposals

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